

## Kalkulus I. (fizika tanári képzés) deriválás gyakorló feladatok megoldás

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$$(1) \left( \frac{\sin(2x)}{\sin(2x) + \cos(2x)} \right)' = \frac{2 \cos(2x)(\sin(2x) + \cos(2x)) - \sin(2x)(2 \cos(2x) - 2 \sin(2x))}{(\sin(2x) + \cos(2x))^2}$$

$$(2) \left( \sqrt{\ln(\cos(x+1))} \right)' = \frac{1}{2} (\ln(\cos(x+1)))^{-\frac{1}{2}} \frac{1}{\cos(x+1)} (-\sin(x+1)) = \frac{-\operatorname{tg}(x+1)}{2\sqrt{\ln(\cos(x+1))}}$$

$$(3) ((1-x) \operatorname{arc} \operatorname{tg}(x^2))' = -\operatorname{arc} \operatorname{tg}(x^2) + (1-x) \frac{1}{1+(x^2)^2} 2x$$

$$(4) \left( \operatorname{arc} \operatorname{tg} \left( \frac{1}{x} \right) \right)' = \frac{1}{1 + \left( \frac{1}{x} \right)^2} (-1)x^{-2} = \frac{-1}{x^2 + 1}$$

$$(5) \left( \sqrt[3]{\sqrt{x^3}\sqrt{x}} \right)' = \left( \sqrt[3]{x^2} \right)' = \frac{2}{3} x^{-\frac{1}{3}} = \frac{2}{3\sqrt[3]{x}}$$

$$(6) (x^3 e^{\sin(3x)})' = 3x^2 e^{\sin(3x)} + x^3 e^{\sin(3x)} 3 \cos(3x)$$

$$(7) \left( \sqrt[4]{\ln(x+2) + 4 \cos\left(\frac{x}{2}\right)} \right)' = \frac{1}{4} (\ln(x+2) + 4 \cos\left(\frac{x}{2}\right))^{-\frac{3}{4}} \left( \frac{1}{x+2} + 4 \cdot \frac{1}{2} (-\sin\left(\frac{x}{2}\right)) \right)$$

$$(8) \left( \ln\left(\frac{x}{3}\right)^2 \right)' = \left( \ln\left(\left(\frac{x}{3}\right)^2\right) \right)' \left( 2 \ln\left(\frac{x}{3}\right) \right)' = \frac{2}{x}$$

$$(9) \left( \ln^2\left(\frac{x}{3}\right) \right)' = \left( \left( \ln\left(\frac{x}{3}\right) \right)^2 \right)' = 2 \ln\left(\frac{x}{3}\right) \frac{1}{x}$$

$$(10) \left( \frac{1}{\sqrt{x}e^{-x^2}} \right)' = \left( x^{-\frac{1}{2}} e^{x^2} \right)' = -\frac{1}{2} x^{-\frac{3}{2}} e^{x^2} + x^{-\frac{1}{2}} e^{x^2} 2x$$